Evaluate.

1. $\displaystyle\int \sin 2x \cos^2 2x \, dx$

2. Find the following limit, if it exists. $\displaystyle\lim_{x \to \infty} (1 - \cos x)$