

Determine if the following series are convergent or divergent. If convergent, find its sum.

$$1. \sum_0^{\infty} \left(\frac{3^n + 2^n}{5^n} \right)$$

$$2. \sum_3^{\infty} \frac{1}{n^2 + 6n + 5}$$

$$3. \sum_1^{\infty} \arccos \frac{1}{n}$$

Evaluate the following improper integrals. If the integral does not exist, state why.

$$4. \int_1^{\infty} \frac{\ln x}{x} dx$$

$$5. \int_1^{\infty} x e^{-x} dx$$